

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Luminescence Intensity Ratio of Lanthanides

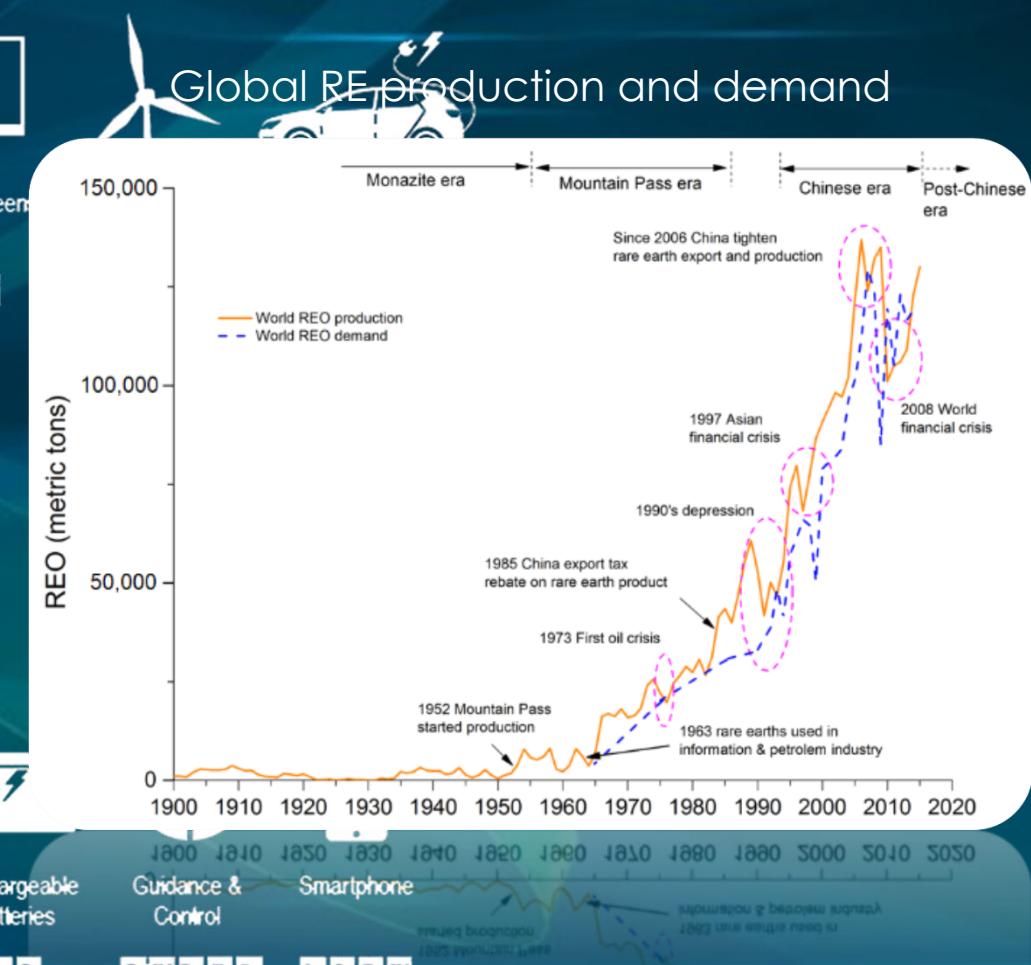
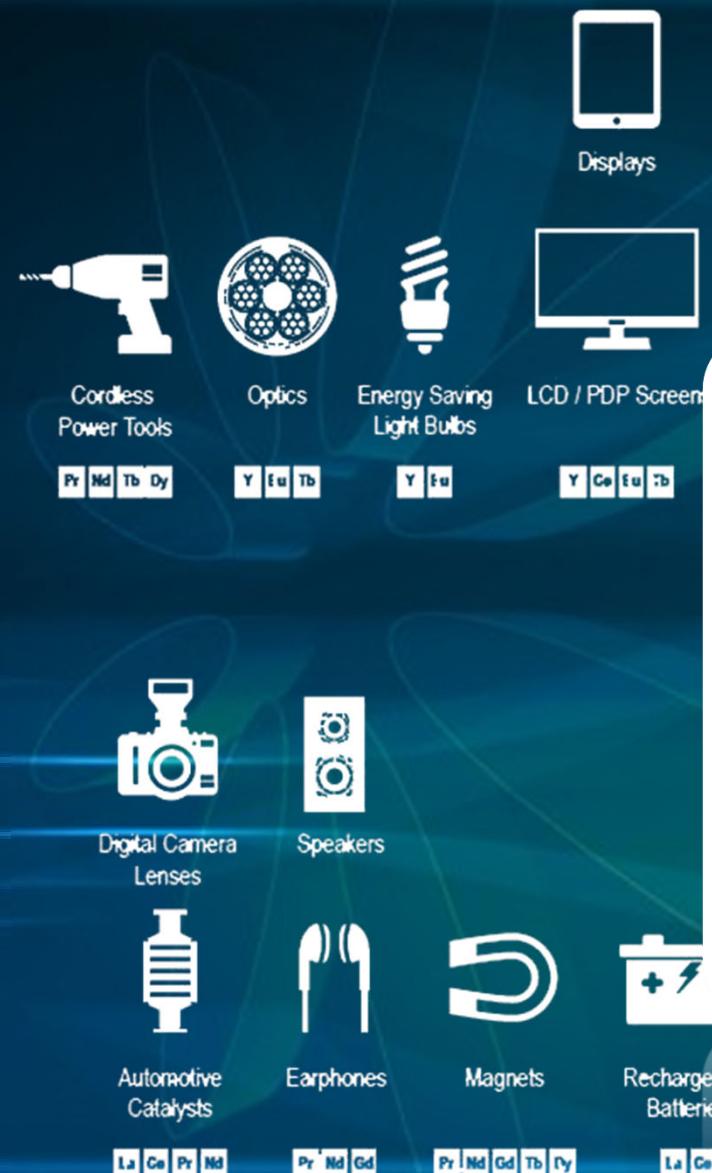
modeling and simulation using
Judd-Ofelt theory

Aleksandar Ćirić

University of Belgrade

OMAS Optical Materials and Spectroscopy Group

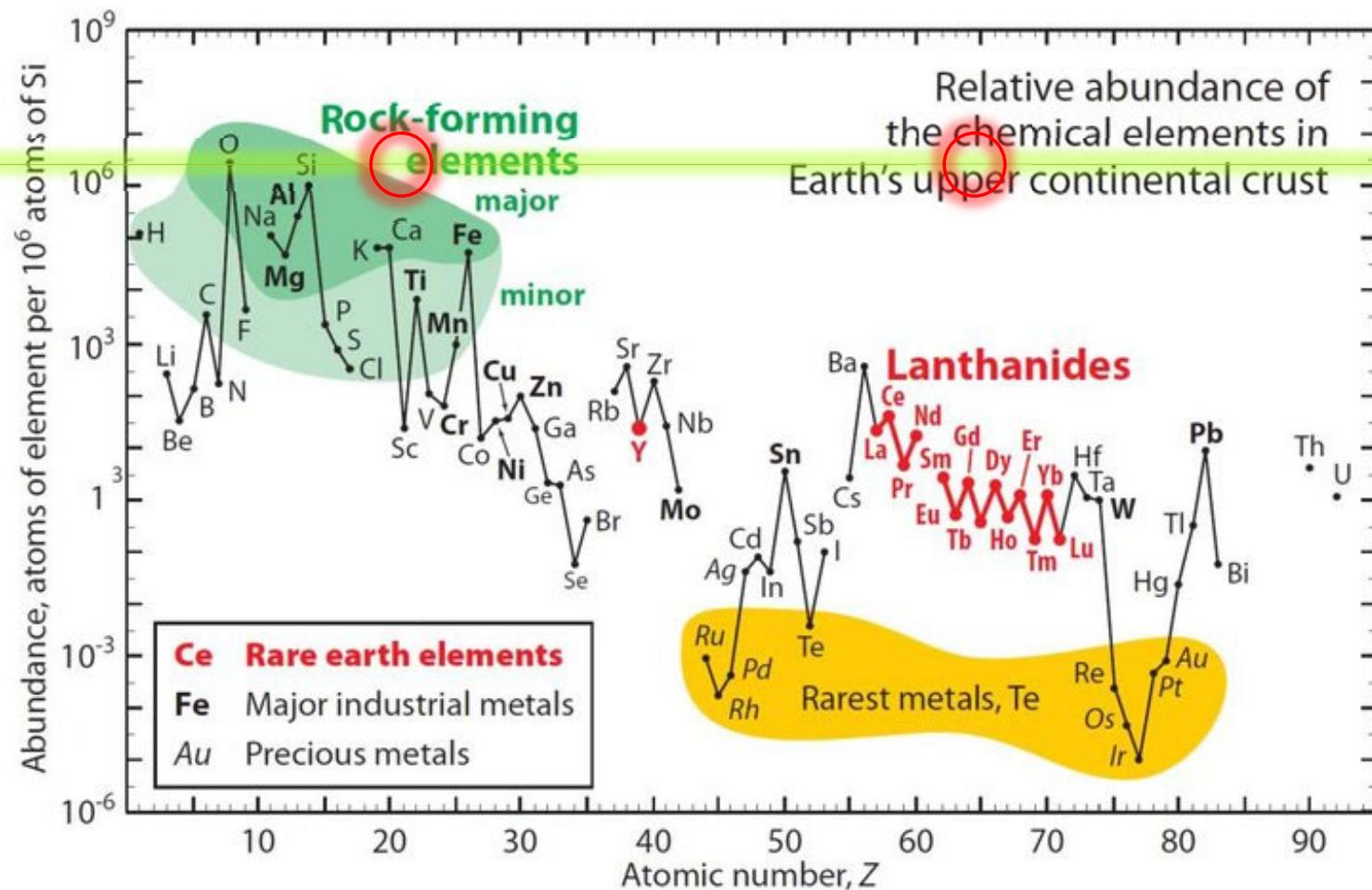
omasgroup.org



Rare-Earth elements

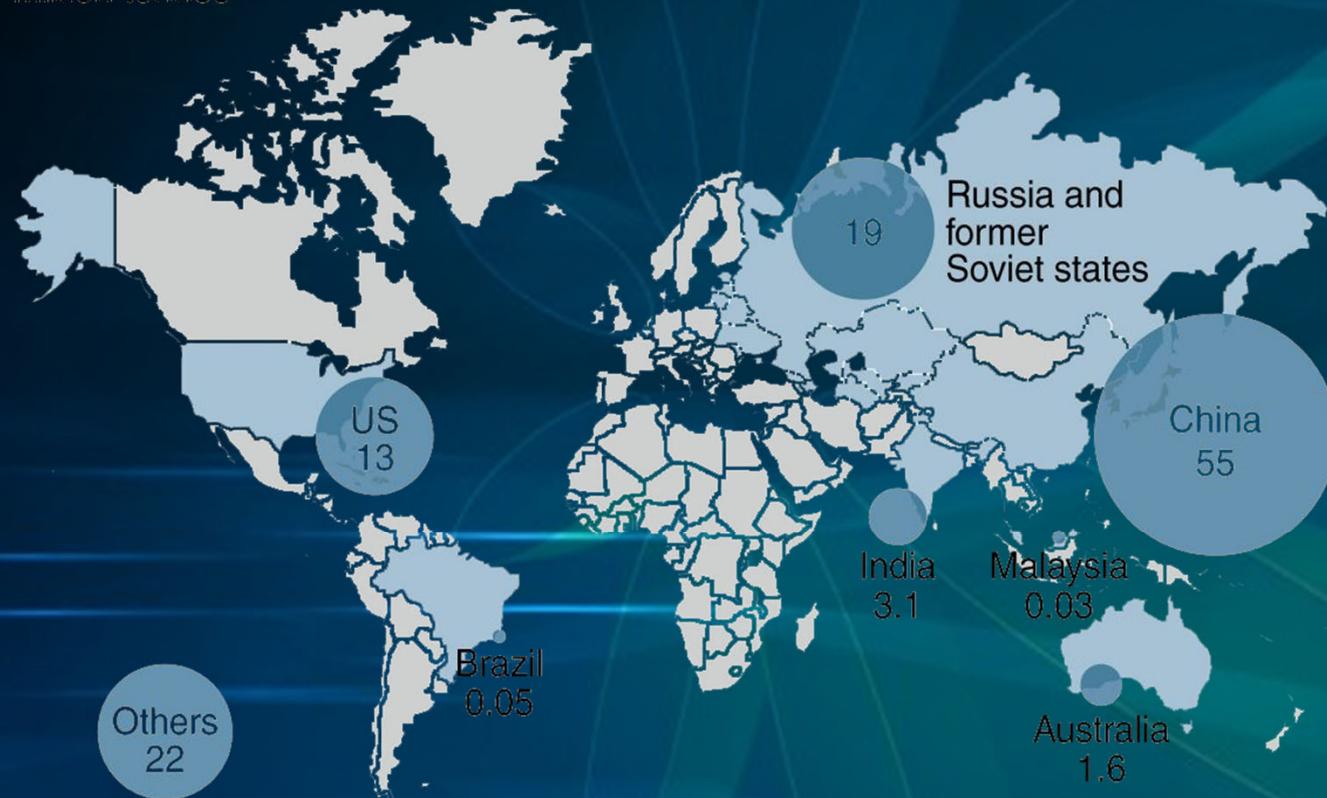
Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18		
Period ↓	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18		
	1 H															2 He				
2	3 Li	4 Be													5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg													13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr		
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe		
6	55 Cs	56 Ba	57 La	* 72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn		
7	87 Fr	88 Ra	89 Ac	* 104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og		
				58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu			
*				90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr			

Abundance



Abundance & Usage

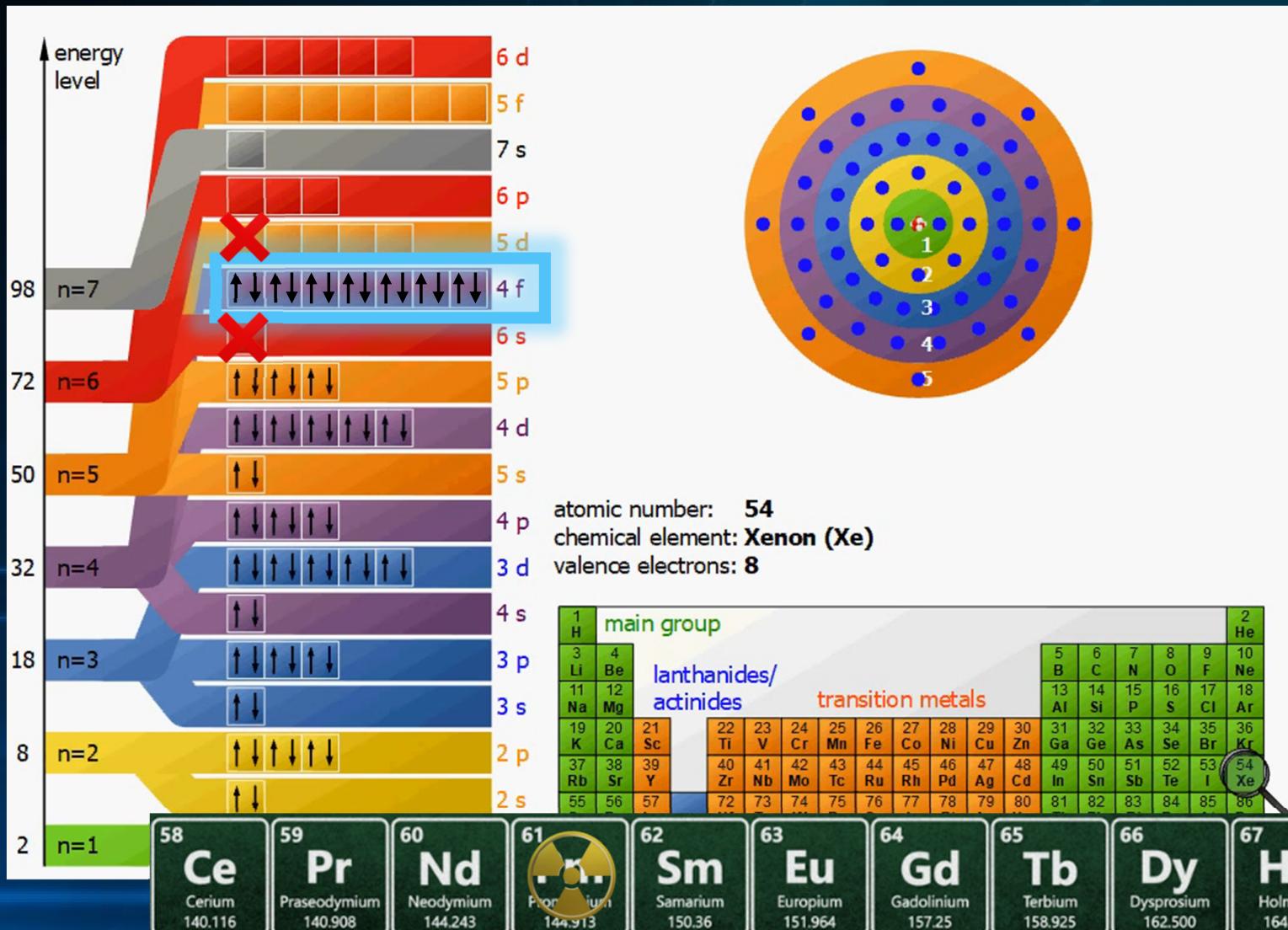
Million tonnes



Phosphors 5%



Lanthanide Electronic Configurations

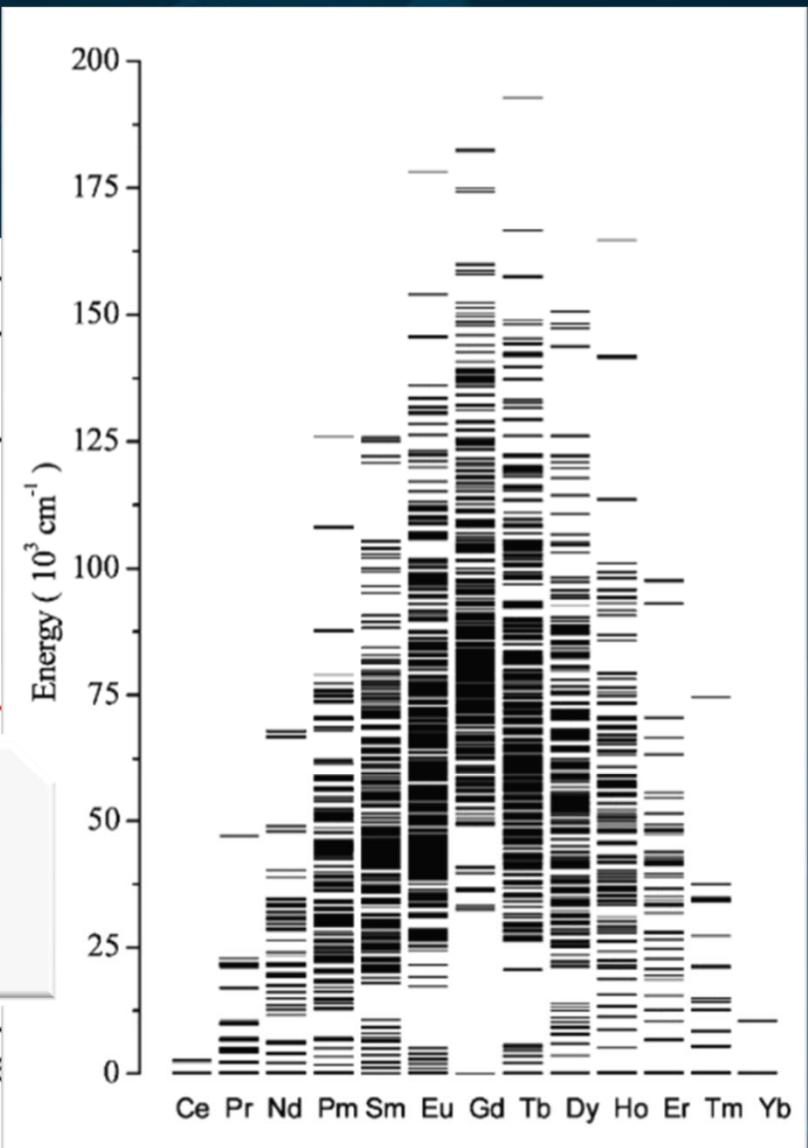
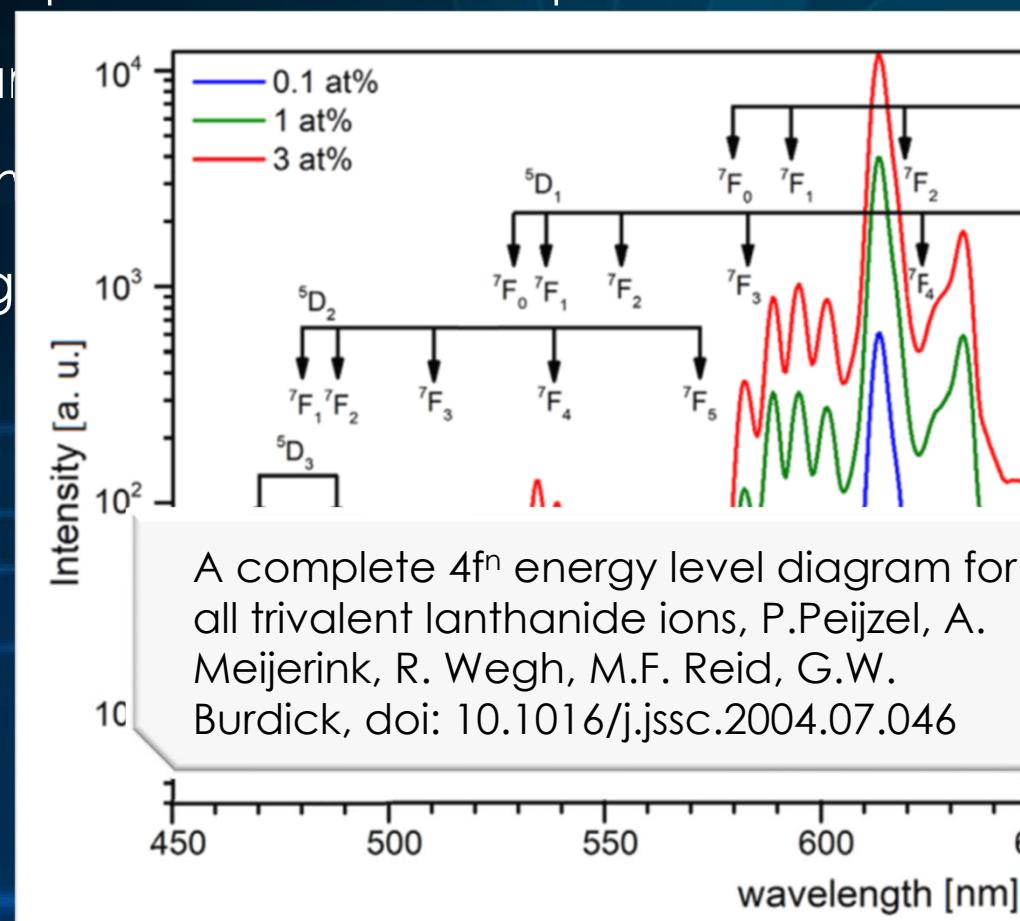


- La = [Xe] 5d¹ 6s²
 - Ce = [La] 4f¹
 - ...
 - Lu = [La] 4f¹⁴
- 3 e⁻
- La³⁺ = [Xe]
 - Ce³⁺ = [Xe] 4f¹
 - ...
 - Lu³⁺ = [Xe] 4f¹⁴

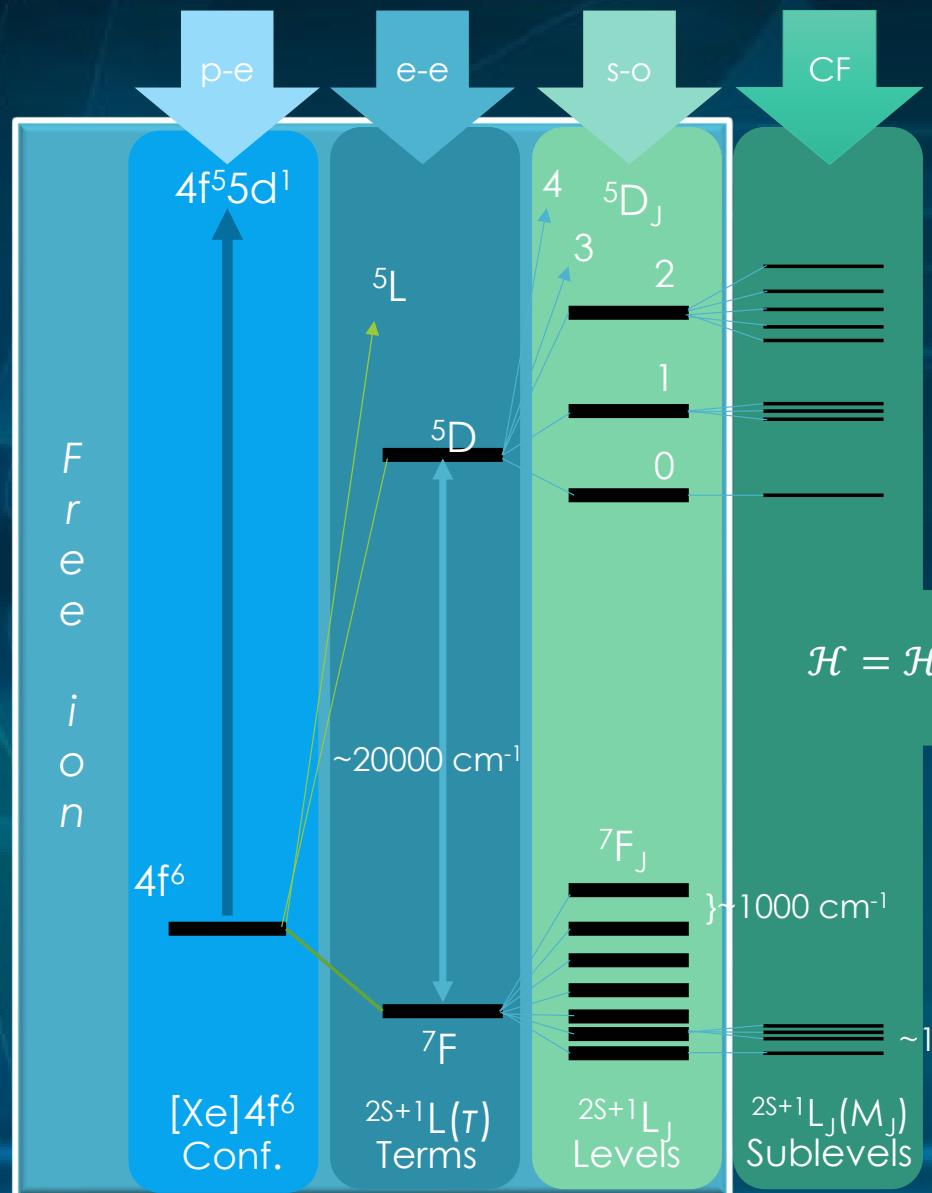
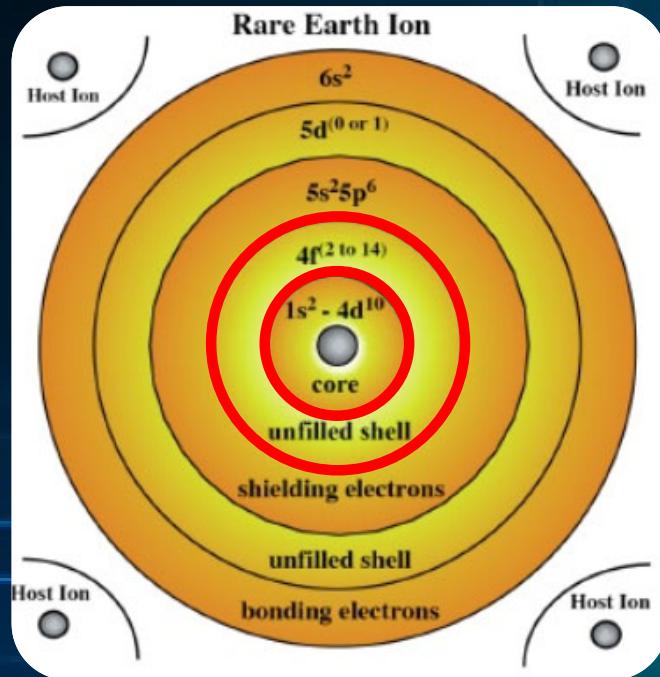
Trivalent Lanthanides

- Sharp emission & absorption lines

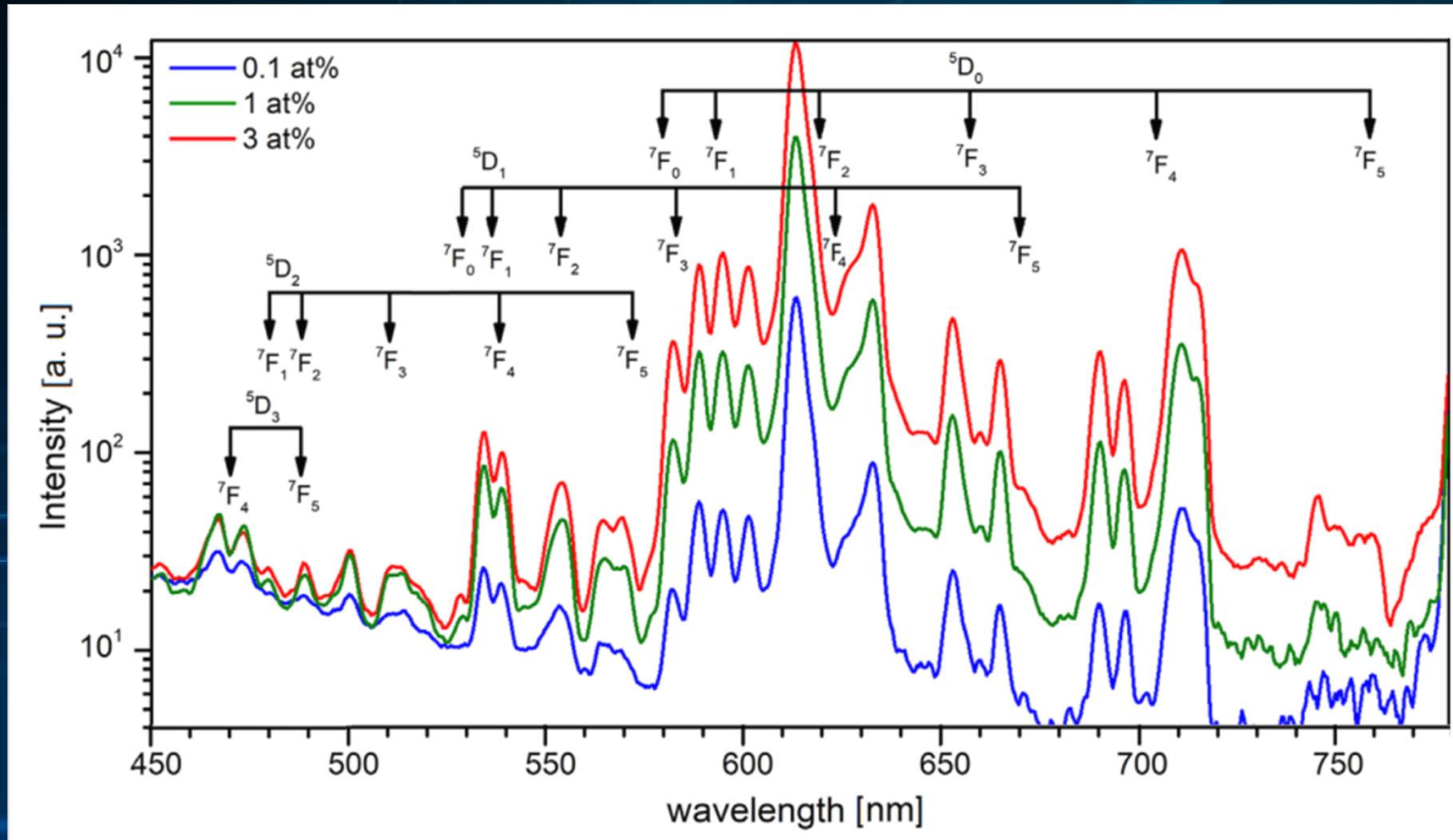
- Transitions
- Longer wavelengths
- Higher concentrations



Ln^{3+} Energy Levels

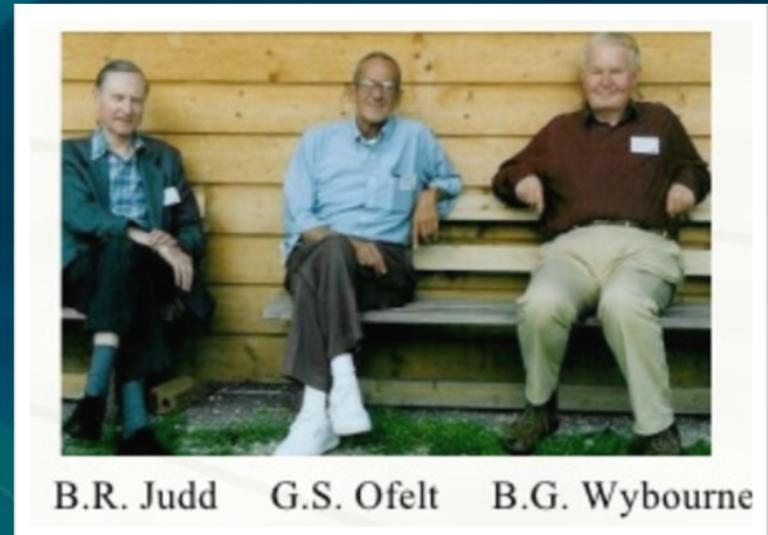


Intensities



Judd-Ofelt theory – Prehistory

- RE discovery: 18th – 20th century
- 1937. – Van Vleck “The Puzzle of RE spectra in solids”
- 1940s - Racah algebra – powerful set of tools that made possible many complex spectroscopic calculations (e.g. free ion energy levels).
- 1959. - Computers – tabulation of angular momentum coupling coefficients.
- 1962. – The solution to the “RE puzzle” simultaneously by Judd and Offelt.



1962.-

University of Belgrade
OMAS group
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PHYSICAL REVIEW

VOLUME 127, NUMBER 3

AUGUST 1, 1962

Optical Absorption Intensities of Rare-Earth Ions

B. R. JUDD

Lawrence Radiation Laboratory, University of California, Berkeley, California

(Received March 12, 1962)

THE JOURNAL OF CHEMICAL PHYSICS

VOLUME 37, NUMBER 3

AUGUST 1, 1962

Intensities of Crystal Spectra of Rare-Earth Ions*

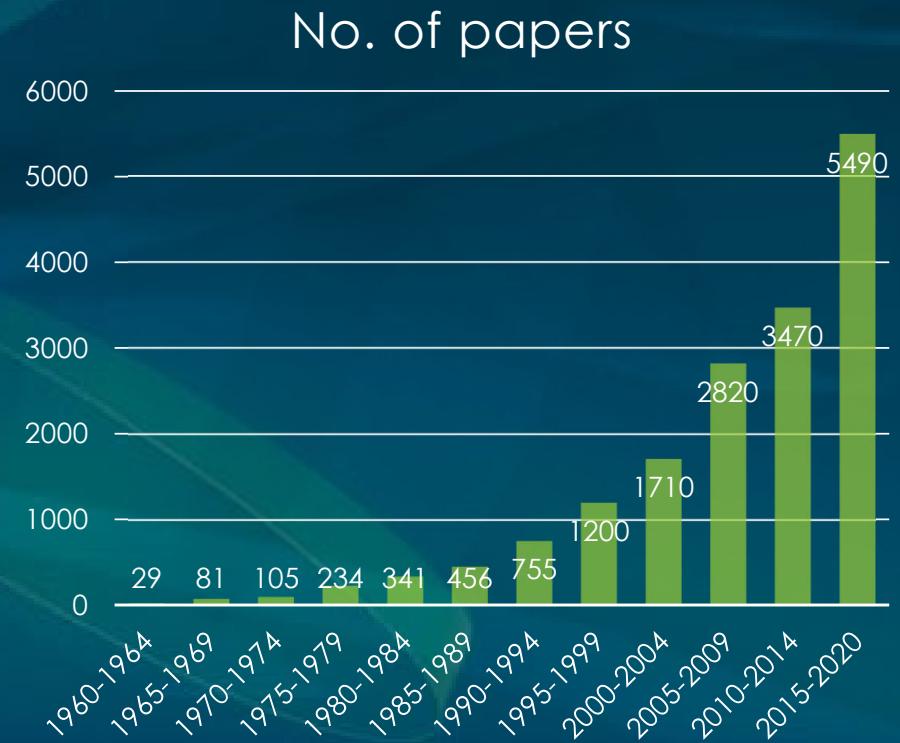
G. S. OFELT

The Johns Hopkins University, Baltimore, Maryland

(Received February 26, 1962)

- “The two papers of 1962 represent the paradigm that has dominated all future work...up to the present time” – B. Wybourne
- Popularity rise
- Very complex QM theory
- Ability to predict oscillator strengths, branching ratios, lifetimes, quantum efficiencies by using only 3 parameters!

$$\Omega$$



Ω_λ Parametrization

Ab Initio



Absorption



Diffuse-
Reflectance,
Excitation



Emission



Ω

Derived
quantities

Application

Ab initio Parametrization

- $\Omega_\lambda = (2\lambda + 1) \sum_p \sum_{t=1,3,5} \frac{|A_{tp}|^2}{2t+1} Y^2(t, \lambda)$
- A_{tp} – parameters of the static CF expansion

- Intensities of 4f-4f Transitions in Glass Materials, O.L. Malta, L.D. Carlos, doi: 10.1590/S0100-40422003000600018
- Judd-Ofelt theory: Principles and Practices, B.M. Walsh, doi: 10.1007/1-4020-4789-4_21
- Judd-Ofelt Theory - The Golden (and the Only One) Theoretical Tool of f-Electron Spectroscopy, L. Smentek, 10.1002/9781118688304.ch10
- Spectral Intensities of f-f transitions, C.G. Walrand, K. Binnemans, doi: 10.1016/S0168-1273(98)25006-9
- Ab-initio calculations of Judd-Ofelt intensity parameters for transitions between crystal-field levels, J.Wen et al., doi: 10.1016/j.jlumin.2013.10.055

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Parametrization from Absorption

- M. Helhen, M. Brik, K. Kramer, 50th anniversary of the Judd-Olfelt theory: An experimentalist's view of the formalism and its application, doi: 10.1016/j.jlumin.2012.10.035
- $f_{\text{exp}} = 4.319 \cdot 10^{-9} \frac{\text{mol}\cdot\text{cm}}{L} \int \varepsilon(\nu) d\nu$
- $f_{\text{abs}} = \frac{8\pi^2 m_e}{3h} \frac{\nu}{2J+1} \frac{\chi_{ED}^{abs}}{n} \sum_{\lambda=2,4,6} \Omega_\lambda |\langle l^N S L J | |U^\lambda| |l^N S' L' J' \rangle|^2 + \frac{h\nu}{6m_e c^2} \frac{n}{2J+1} |\langle l^N S L J | |L + gS| |l^N S' L' J' \rangle|^2$
- RELIC software
- Problems: “This method has two drawbacks: the density of ions in the sample must be accurately measured, and absorption can only be performed on single crystals and glasses but not on crystalline powders”, Blasse, doi: 10.1063/1.457106

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Parametrization from Excitation or DR

- Determination of Judd-Ofelt intensity parameters from the excitation spectra for rare-earth doped luminescent materials, W. Luo et al., doi: 10.1039/b921581f
- $S_{ex} = \frac{c}{\lambda\chi} \Gamma_{ex}$, $S_{th} = \sum_{\lambda=2,4,6} \Omega_\lambda |\langle l^N S L J | | U^\lambda | | l^N S' L' J' \rangle|^2 \Rightarrow \Omega_2 : \Omega_4 : \Omega_6$
- For absolute values calibration is needed!
- $\tau_r^{-1} = \sum A_{J'}$
- Problem: Assumption that the non-radiative lifetime of the used level is 0!
- Xue et al. Validity of Judd-Ofelt spectroscopy based on diffuse reflectance spectrum and fluorescence lifetime of phosphor, doi: 10.1016/j.jlumin.2020.117304

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Parametrization from Emission: Gd³⁺

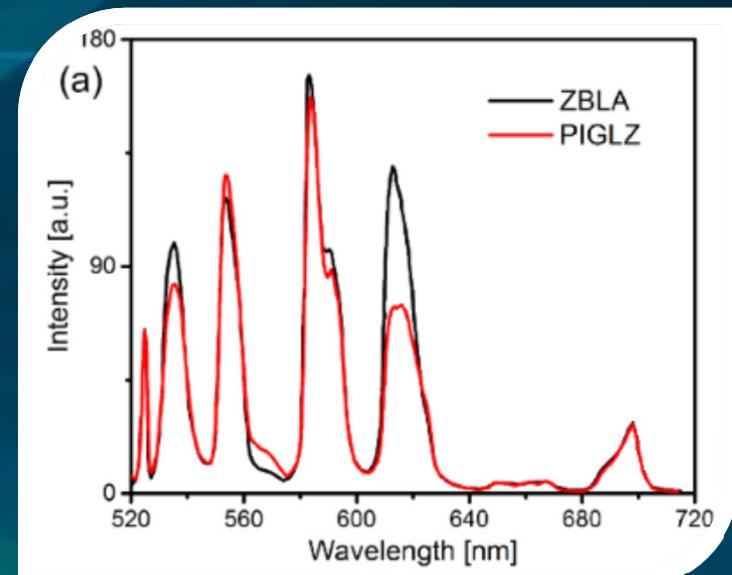
- The spectroscopy of Gd³⁺ in yttriumoxychloride: Judd-Ofelt parameters from emission data, J. Sytsma, G.F. Imusch, G. Blasse, doi: 10.1063/1.457106
- Similar to excitation, but by using A_{J'}

$$A_{SLJ \rightarrow S'L'J'} = \frac{64\pi^4 \tilde{\nu}_{SLJ \rightarrow S'L'J'}^3}{3h(2J+1)} (\chi_{ED} D_{ED} + \chi_{MD} D_{MD})$$
$$\tau_R = 1 / \sum A_{SLJ \rightarrow S'L'J'}$$

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Parametrization from Emission: Eu³⁺ - Introduction

- Krupke, William F. "Optical absorption and fluorescence intensities in several rare-earth-doped Y₂O₃ and LaF₃ single crystals." *Physical Review* 145.1 (1966): 325.
 - MD – host independent – can be used for calibration.
 - $^5D_0 \rightarrow ^7F_1$
- Judd-Ofelt parametrization from emission spectra:
The case study of the Eu³⁺ 5D_1 emitting level, A. Ćirić, S. Stojadinović, M.G. Brik, M.D. Dramićanin, doi: 10.1016/j.chemphys.2019.110513
 - New: $^5D_1 \rightarrow ^7F_0$



58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Parametrization from Emission: Eu³⁺

$$A_{SLJ \rightarrow S'L'J'} = \frac{64\pi^4 \tilde{\nu}_{SLJ \rightarrow S'L'J'}^3}{3h(2J+1)} (\chi_{ED} D_{ED} + \chi_{MD} D_{MD})$$

Baricenter
Local field correction
Dipole strength

$$I_{SLJ \rightarrow S'L'J'} = \int i_{SLJ \rightarrow S'L'J'}(\tilde{\nu}) d\tilde{\nu} = h\tilde{\nu}_{SLJ \rightarrow S'L'J'} N_{SLJ} A_{SLJ \rightarrow S'L'J'}$$

Population
 \rightarrow
 $\frac{I_\lambda}{I_{MD}} = \frac{\tilde{\nu}_\lambda A_\lambda}{\tilde{\nu}_{MD} A_{MD}} = \left(\frac{\tilde{\nu}_\lambda}{\tilde{\nu}_{MD}}\right)^4 \frac{\chi_{ED} D_{ED}^\lambda}{\chi_{MD} D_{MD}}$

\downarrow

$$\Omega_\lambda = \frac{D_{MD}}{e^2 U^\lambda} \left(\frac{\tilde{\nu}_{MD}}{\tilde{\nu}_\lambda}\right)^4 \frac{9n_{MD}^3}{n_\lambda(n_\lambda^2 + 2)^2} \frac{I_\lambda}{I_{MD}}$$

\leftarrow

$D_{ED}^\lambda = e^2 \Omega_\lambda U^\lambda$

RME

58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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Pa

JOES - Judd-Ofelt from Emission Spectra

File Help

Input

Refractive Index
User defined

Overall Quantum Yield **Observation**

Data for Branching Ratio
Not necessary for other calculations

${}^5D_0 \rightarrow {}^7F_0$ min [nm] max [nm]
 ${}^5D_0 \rightarrow {}^7F_3$
 ${}^5D_0 \rightarrow {}^7F_5$

${}^5D_0 \rightarrow {}^7F_1$ min [nm] max [nm]
 ${}^5D_0 \rightarrow {}^7F_2$
 ${}^5D_0 \rightarrow {}^7F_4$
 ${}^5D_0 \rightarrow {}^7F_6$

Wavelength range ${}^5D_0 \rightarrow {}^7F_0$
 ${}^7F_3: 640 - 660, {}^7F_4: 680 - 710$

Symmetry - Europium as a spectroscopic probe
Number of emission bands for term

7F_0 0 7F_1 0 7F_2 0 7F_3 0 7F_4 0 7F_5 0 7F_6 0

Judd-Ofelt Parameters:
 $\Omega_2 = 1.1465194020534921E-19 \text{ cm}^2$
 $\Omega_4 = 2.9751146626870955E-20 \text{ cm}^2$
 $\Omega_6 = \text{NaN cm}^2$

== Derived Quantities ==
Radiative Transition Probabilities
 $A({}^5D_0 \rightarrow {}^7F_1) = 68.17799738106247 \text{ s}^{-1}$
 $A({}^5D_0 \rightarrow {}^7F_2) = 490.78769879104266 \text{ s}^{-1}$
 $A({}^5D_0 \rightarrow {}^7F_4) = 63.78022107243416 \text{ s}^{-1}$
 $A({}^5D_0 \rightarrow {}^7F_6) = \text{NaN s}^{-1}$

Experimental Branching Ratios and Theoretical Branching Ratios
 $\beta({}^5D_0 \rightarrow {}^7F_1) = 0.11452264749042913; 0.10947963767105741$
 $\beta({}^5D_0 \rightarrow {}^7F_2) = 0.7938046817756628; 0.7881026357629585$
 $\beta({}^5D_0 \rightarrow {}^7F_4) = 0.09167267073390804; 0.10241772656598405$
 $\beta({}^5D_0 \rightarrow {}^7F_6) = 0.0; 0.0$

Barycenters
 $v({}^5D_0 \rightarrow {}^7F_1) = 16858.597021525726 \text{ cm}^{-1}$
 $v({}^5D_0 \rightarrow {}^7F_2) = 16232.818864281908 \text{ cm}^{-1}$
 $v({}^5D_0 \rightarrow {}^7F_4) = 14425.398497300715 \text{ cm}^{-1}$
 $v({}^5D_0 \rightarrow {}^7F_6) = \text{NaN cm}^{-1}$

Total Radiative transition probability = $622.7459172445393 \text{ s}^{-1}$
Nonradiative transition probability = 0.0 s^{-1}

Lifetimes
Theoretical radiative lifetime = $0.0016530641897090424 \text{ s}$
Calculated radiative lifetime = $0.0016057913385039838 \text{ s}$

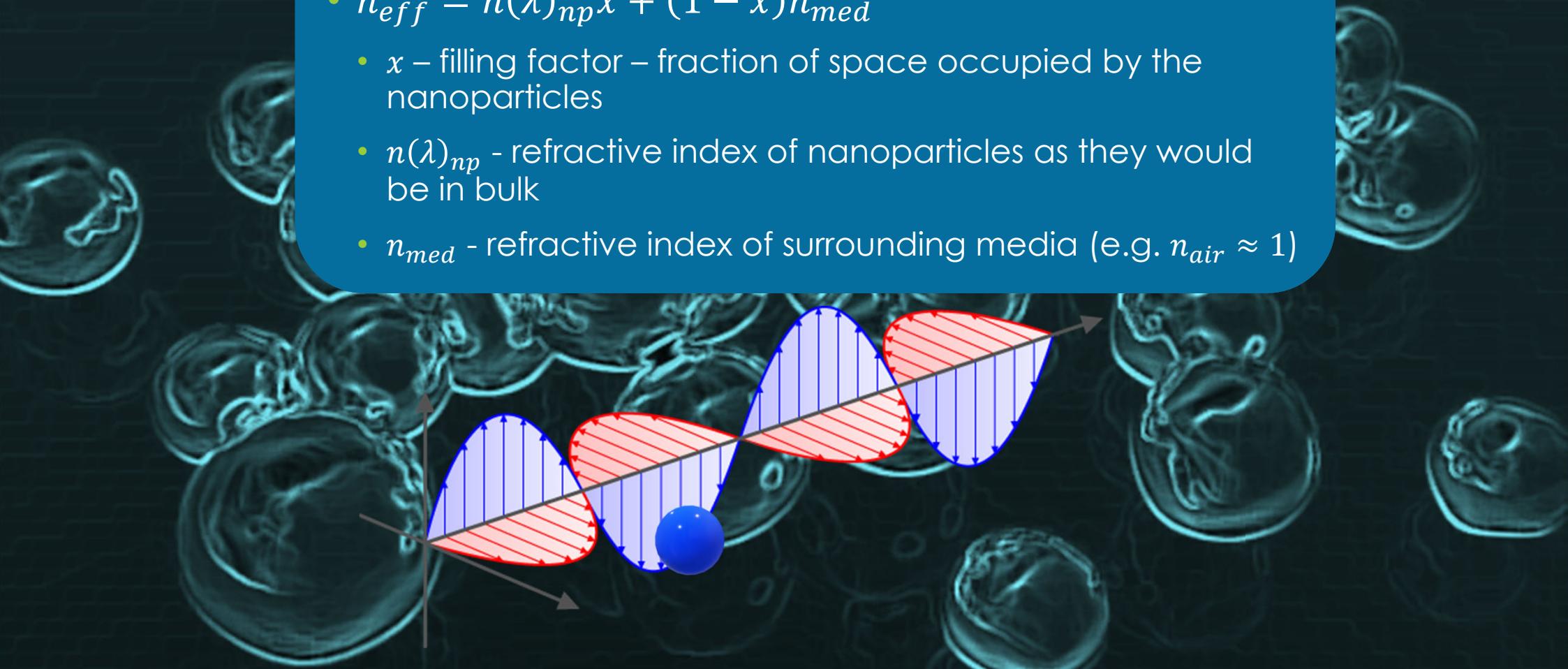
Calculate

another calculation
n.2018.09.048

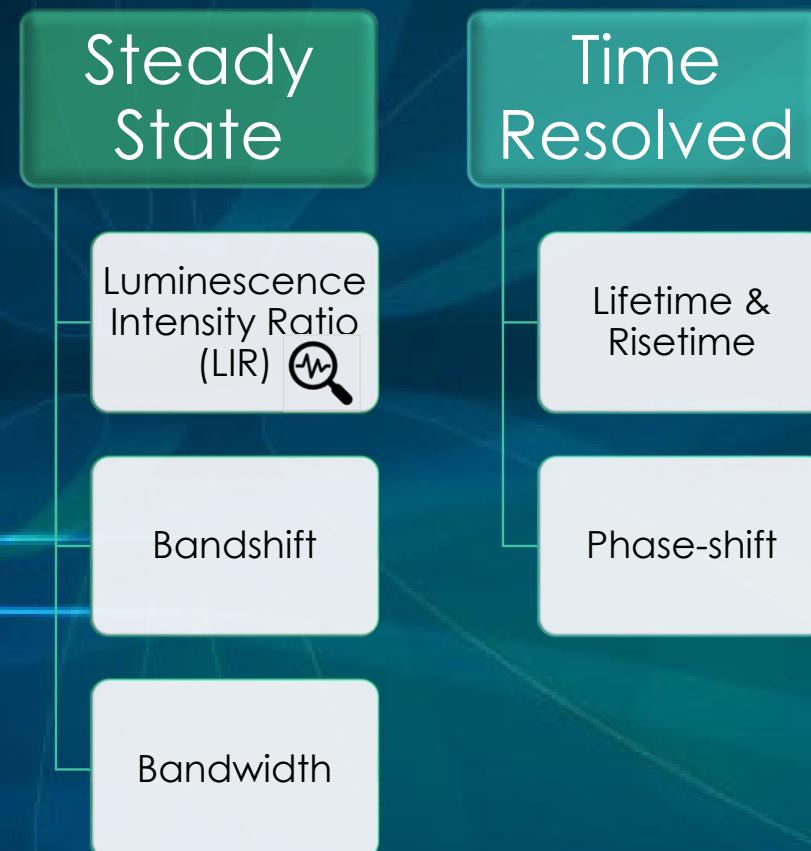
b
ium
155

Nanomaterials

- Correction for nanocrystals $\ll \lambda$
- $n_{eff} = n(\lambda)_{np}x + (1 - x)n_{med}$
 - x – filling factor – fraction of space occupied by the nanoparticles
 - $n(\lambda)_{np}$ - refractive index of nanoparticles as they would be in bulk
 - n_{med} - refractive index of surrounding media (e.g. $n_{air} \approx 1$)



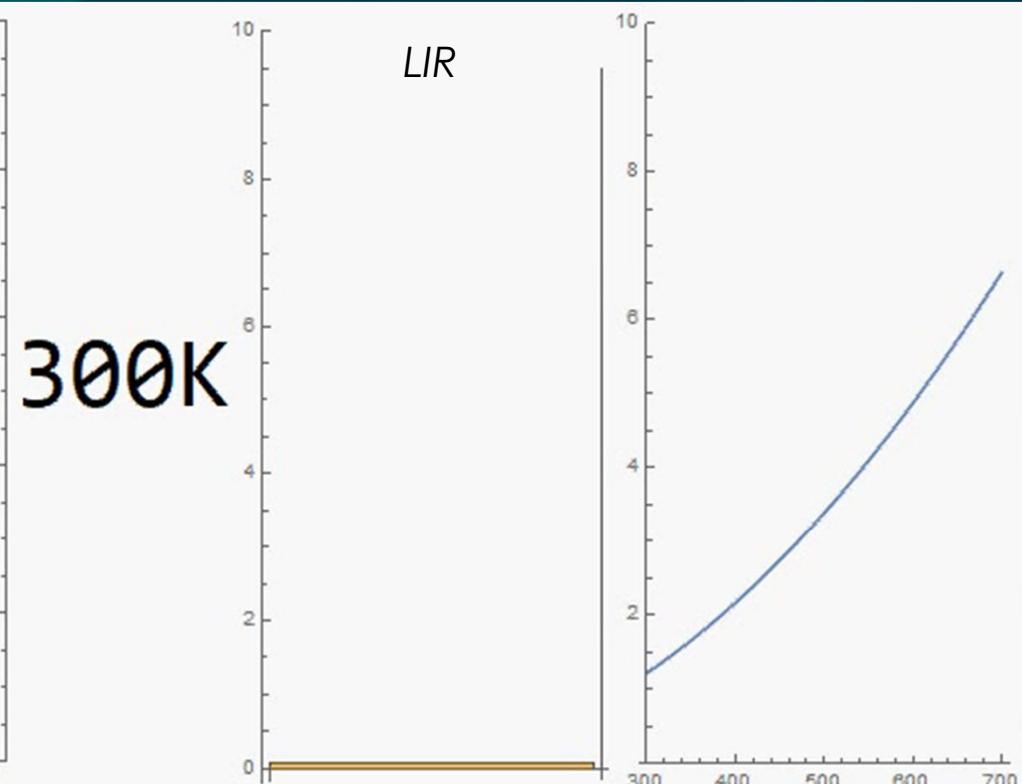
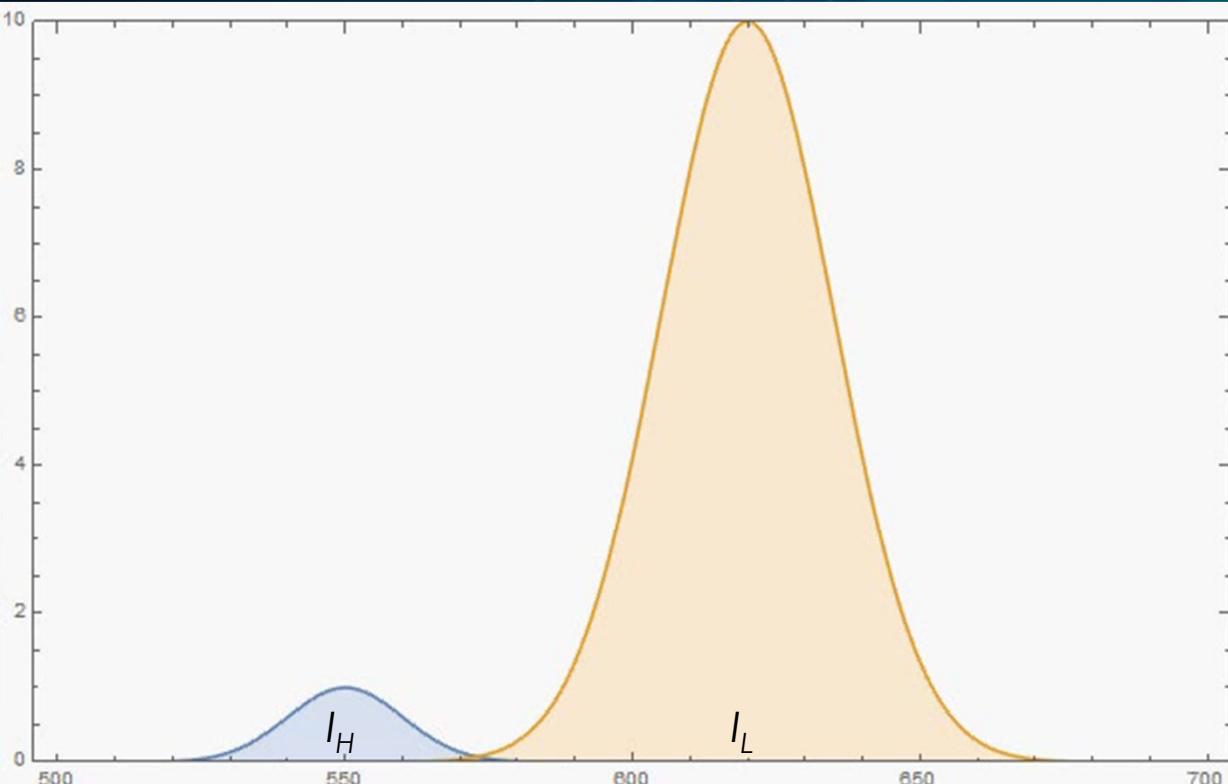
Luminescence thermometry



Luminescence Intensity Ratio (LIR)

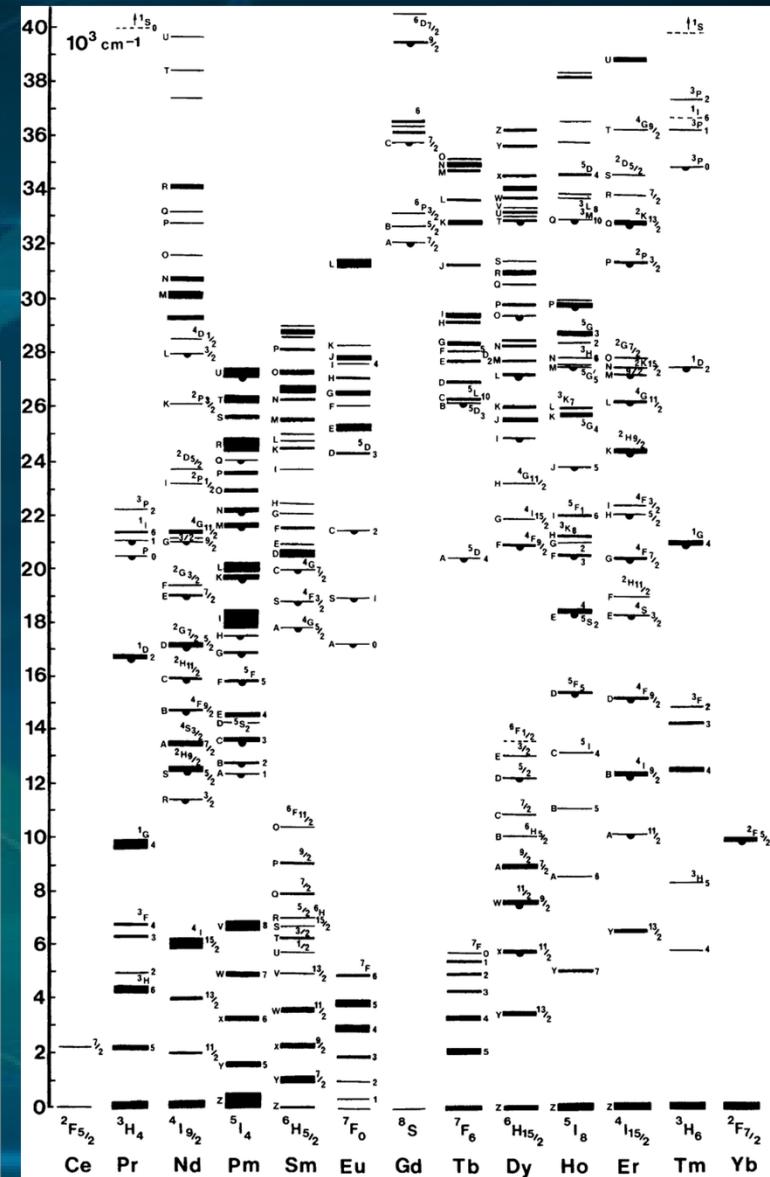
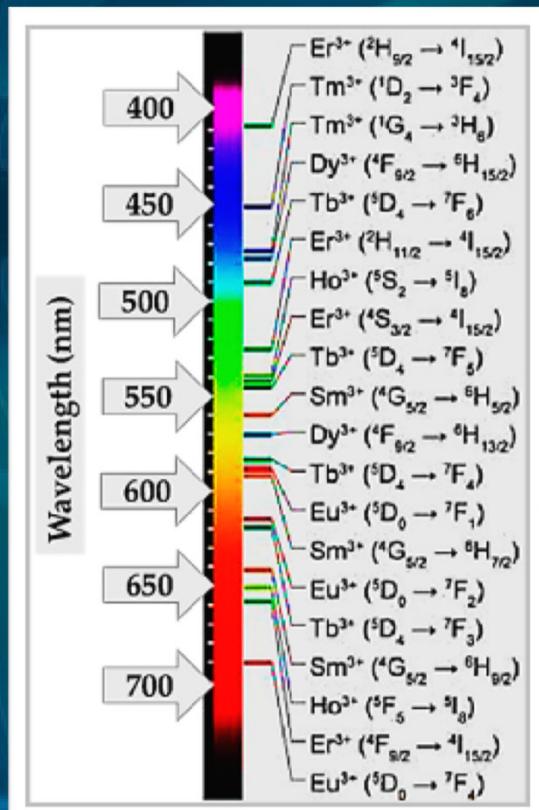
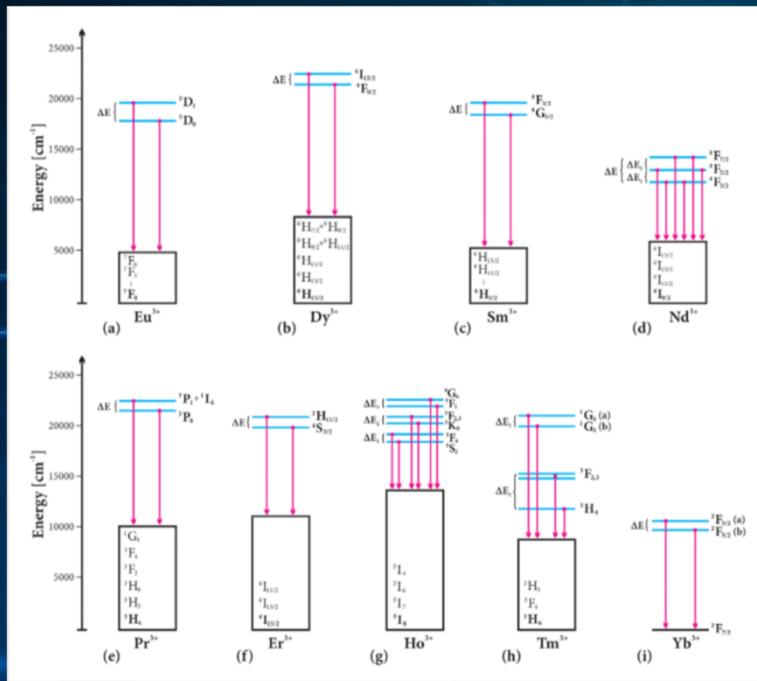
The most widely used method!

$$LIR = \frac{I_H}{I_L} = \left| \frac{N_H}{N_L} = \frac{g_H}{g_L} e^{-\Delta E/kT} \right| = B e^{-\Delta E/kT}$$



LIR & Ln

- Abundance of sharp emissions to chose from, from UV to IR!
- Many of them are intense!
- Many well thermalized levels!



Judd-Ofelt and LIR: Acknowledgments

- Can JO be applied to LIR thermometry?
- Upconverting Nanoparticles Working As Primary Thermometers in Different Media, S. Balabhadra, M.L. Debasu, C.Brites, R.Ferreira, L.D. Carlos, doi:10.1021/acs.jpcc.7b04827
- A Novel Multifunctional Upconversion Phosphor: $\text{Yb}^{3+}/\text{Er}^{3+}$ Codoped La_2S_3 , Y.Yang et al., doi: 10.1111/jace.12822

Judd-Ofelt and LIR

$$LIR = \frac{I_H}{I_L} = \left| I = h\tilde{\nu}NA, \frac{N_H}{N_L} = \frac{g_H}{g_L} e^{-\frac{\Delta E}{kT}} \right| = \frac{h\tilde{\nu}_H N_H A_H}{h\tilde{\nu}_L N_L A_L} = \underbrace{\frac{g_H h\tilde{\nu}_H A_H}{g_L h\tilde{\nu}_L A_L}}_B e^{-\frac{\Delta E}{kT}}$$

$$A_{SLJ \rightarrow S'L'J'} = \frac{64\pi^4 \tilde{\nu}_{SLJ \rightarrow S'L'J'}^3}{3h(2J+1)} (\chi_{ED} D_{ED} + \chi_{MD} D_{MD}) \quad + \quad B = \frac{g_H h\tilde{\nu}_H A_H}{g_L h\tilde{\nu}_L A_L} \quad \rightarrow \quad B = \left(\frac{\tilde{\nu}_H}{\tilde{\nu}_L} \right)^4 \frac{\chi_{ED}^H D_{ED}^H + \chi_{MD}^H D_{MD}^H}{\chi_{ED}^L D_{ED}^L + \chi_{MD}^L D_{MD}^L}$$

U^λ and D_{MD} are tabulated and host independent

$$D_{ED}^\lambda = e^2 \sum_\lambda \Omega_\lambda U^\lambda$$

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Figures of Merit via Ω_λ

$$S(T) = \frac{\Delta E}{kT^2} B \exp\left(-\frac{\Delta E}{kT}\right) = \frac{\Delta E}{kT^2} \left(\frac{\tilde{v}_H}{\tilde{v}_L}\right)^4 \frac{\chi_{ED}^H D_{ED}^H + \chi_{MD}^H D_{MD}^H}{\chi_{ED}^L D_{ED}^L + \chi_{MD}^L D_{MD}^L} \exp\left(-\frac{\Delta E}{kT}\right)$$

$$S_{max} = \frac{4k}{e^2 \Delta E} \left(\frac{\tilde{v}_H}{\tilde{v}_L}\right)^4 \frac{\chi_{ED}^H D_{ED}^H + \chi_{MD}^H D_{MD}^H}{\chi_{ED}^L D_{ED}^L + \chi_{MD}^L D_{MD}^L}$$

$$\Delta T = \frac{kT^2 \sigma (\chi_{ED}^L D_{ED}^L + \chi_{MD}^L D_{MD}^L)}{\Delta E (\chi_{ED}^H D_{ED}^H + \chi_{MD}^H D_{MD}^H) \exp(-\Delta E/kT)}$$

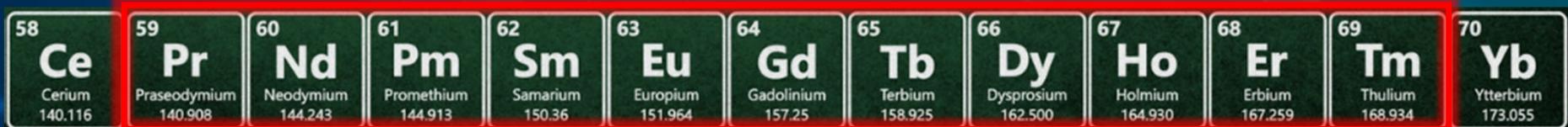
An Extension of the Judd-Ofelt theory to the field of lanthanide thermometry, A. Ćirić, S. Stojadinović, M.D. Dramićanin, doi: 10.1016/j.jlumin.2019.116749

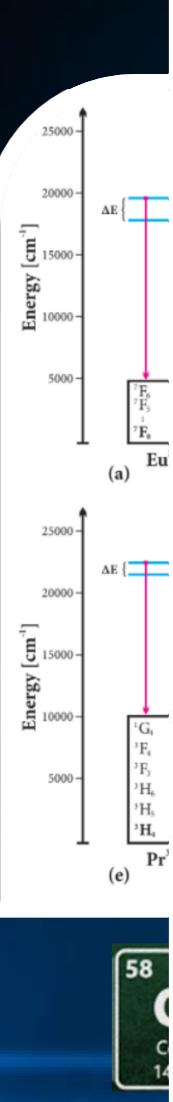
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Significance

- Ω_λ is easier to obtain (single spectrum @ RT)
- Large number of Ω_λ in literature
 - Largest #: Spectral Intensities of f-f transitions, C.G. Walrand, K. Binnemans, doi: 10.1016/S0168-1273(98)25006-9

	JO-LIR	Experimental
Setup Price	Low	High
Speed	High	Low
Knowledge Level	Mid	High
Accuracy	Mid	High



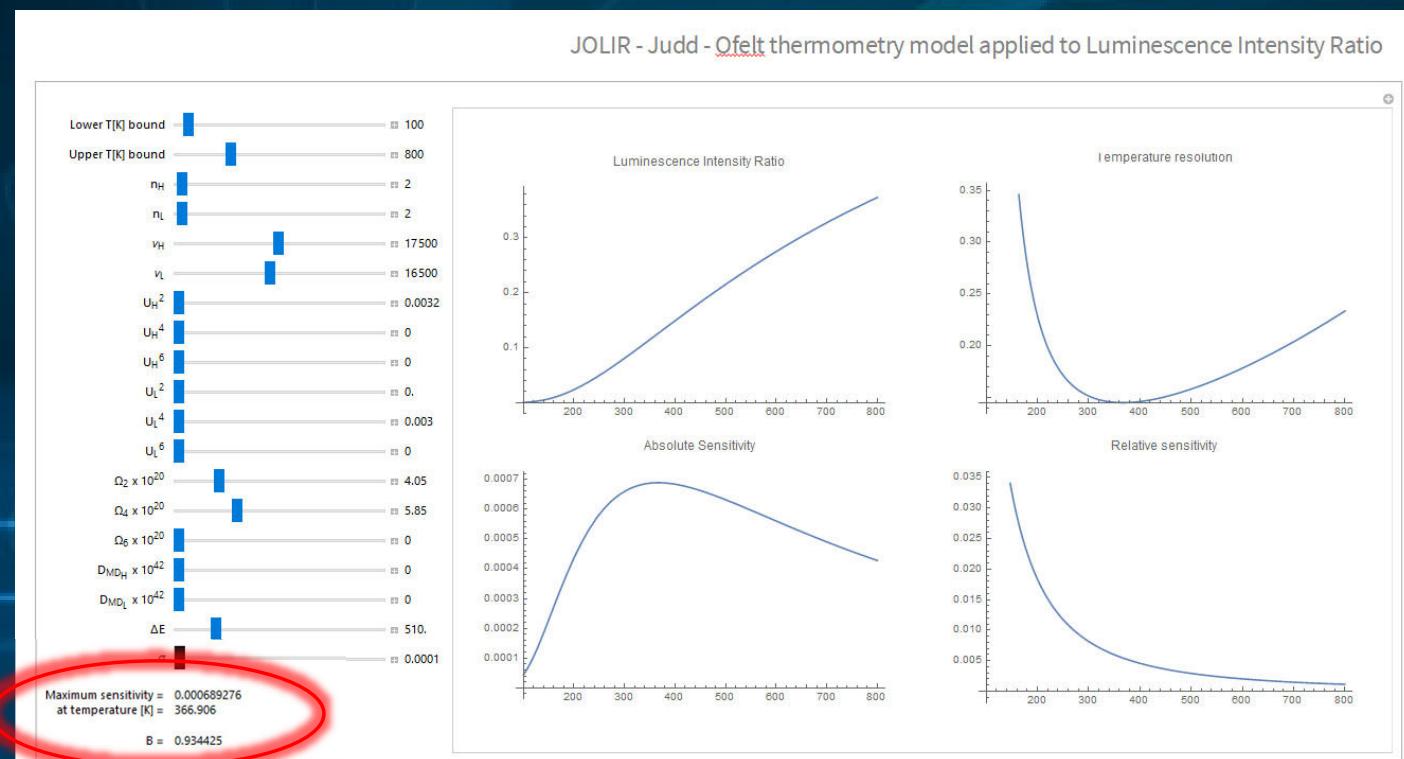


Transition	High or Low	λ [nm]	U^2	U^4	U^6	$D_{MD} \cdot 10^{42}$ [esu ² cm ²]	$\chi_{ED}D_{ED} + \chi_{MD}D_{MD}$ [esu ² cm ²]
Pr³⁺ [57,58]							
³ P ₁ → ³ H ₅	H	525	0	0.2857	0.0892	0	$\eta(0.2857\Omega_4 + 0.0892\Omega_6)$
³ P ₀ → ³ H ₅	L	540	0	0	0	0	0
Nd³⁺ [46,47]							
⁴ F _{7/2} → ⁴ I _{9/2}	H	740	0.0011	0.0406	0.4272	$\approx 0^c$	$\eta(0.0011\Omega_2 + 0.0406\Omega_4 + 0.4272\Omega_6)$
⁴ F _{5/2} → ⁴ I _{9/2}	H or L	815	0.0006	0.2337	0.3983	0	$\eta(0.0006\Omega_2 + 0.2337\Omega_4 + 0.3983\Omega_6)$
⁴ F _{3/2} → ⁴ I _{9/2}	L	900	0	0.2283	0.0554	0	$\eta(0.2283\Omega_4 + 0.0554\Omega_6)$
⁴ F _{7/2} → ⁴ I _{11/2}	L	1075	0.0009	0.2335	0.3076	0	$\eta(0.0009\Omega_2 + 0.2335\Omega_4 + 0.3076\Omega_6)$
Sm³⁺							
⁴ F _{3/2} → ⁶ H _{5/2}	H	530	0.00003 ^a	0.00008 ^a	0	0.3 ^c	$\eta(0.00003\Omega_2 + 0.00008\Omega_4) + n^3 \cdot 0.2 \cdot 10^{-42}$
⁴ G _{5/2} → ⁶ H _{5/2}	L	560	0.0004 ^a	0.0001 ^a	0	12.2 ^c	$\eta(0.0004\Omega_2 + 0.0001\Omega_4) + n^3 \cdot 0.8 \cdot 10^{-42}$
⁴ G _{5/2} → ⁶ H _{7/2}	L	587	0	0.0078	0.0075	12.2 ^c	$\eta(0.0078\Omega_4 + 0.0075\Omega_6) + n^3 \cdot 1.3 \cdot 10^{-42}$
⁴ G _{5/2} → ⁶ H _{9/2}	L	650	0.0096	0.0061	0.0019	0	$\eta(0.0096\Omega_2 + 0.0061\Omega_4 + 0.0019\Omega_6)$
⁴ G _{5/2} → ⁶ H _{11/2}	L	710	0	0.0045	0.0018	0	$\eta(0.0045\Omega_4 + 0.0018\Omega_6)$
Eu³⁺ ^a							
⁵ D ₁ → ⁷ F ₁	H	535	0.0026	0	0	$\approx 0^c$	$\eta \cdot 0.0026\Omega_2$
⁵ D ₁ → ⁷ F ₂	H	555	0.0008	0	0	11.2	$\eta \cdot 0.0008\Omega_2 + n^3 \cdot 11.2 \cdot 10^{-42}$
⁵ D ₀ → ⁷ F ₁	L	585	0	0	0	9.6	$n^3 \cdot 9.6 \cdot 10^{-42}$
⁵ D ₀ → ⁷ F ₂	L	612	0.0032	0	0	0	$\eta \cdot 0.0032\Omega_2$
⁵ D ₀ → ⁷ F ₄	L	695	0	0.0023	0	0	$\eta \cdot 0.0023\Omega_4$
Dy³⁺							
⁴ I _{15/2} → ⁶ H _{15/2}	H	455	0.0071	0.0003	0.0659	82.3 ^c	$\eta(0.0071\Omega_2 + 0.0003\Omega_4 + 0.0659\Omega_6) + n^3 \cdot 9.0 \cdot 10^{-42}$
⁴ F _{9/2} → ⁶ H _{15/2}	L	490	0	0.0046	0.0292	0	$\eta(0.0046\Omega_4 + 0.0292\Omega_6)$
⁴ F _{9/2} → ⁶ H _{13/2}	L	570	0.0490	0.0164	0.0545	0	$\eta(0.0490\Omega_2 + 0.0164\Omega_4 + 0.0545\Omega_6)$
⁴ F _{9/2} → ⁶ H _{11/2}	L	660	0.0093	0.0018	0.0033	26.3 ^c	$\eta(0.0093\Omega_2 + 0.0018\Omega_4 + 0.0033\Omega_6) + n^3 \cdot 27.5 \cdot 10^{-42}$
⁴ F _{9/2} → ⁶ H _{9/2}	L	735	0.0021	0.0024	0.0032	8.9 ^c	$\eta(0.0021\Omega_2 + 0.0024\Omega_4 + 0.0032\Omega_6) + n^3 \cdot 8.9 \cdot 10^{-42}$
Ho³⁺ ^b							
⁵ F ₄ → ⁷ I ₈	H	530	0	0.2385	0.7090	0	$\eta(0.2385\Omega_4 + 0.7090\Omega_6)$
⁵ S ₂ → ⁷ I ₈	H or L	545	0	0	0.2145	0	$\eta \cdot 0.2145\Omega_6$
⁵ F ₄ → ⁷ I ₇	H or L	750	0	0.1965	0.0320	0	$\eta(0.1965\Omega_4 + 0.0320\Omega_6)$
⁵ S ₂ → ⁷ I ₇	L	710	0	0	0.4195	0	$\eta \cdot 0.4195\Omega_6$
Er³⁺ ^a							
² H _{11/2} → ⁴ I _{15/2}	H	525	0.5977	0.3456	0.0790	0	$\eta(0.5977\Omega_2 + 0.3456\Omega_4 + 0.0790\Omega_6)$
⁴ S _{3/2} → ⁴ I _{15/2}	L	550	0	0	0.2119	0	$\eta \cdot 0.2119\Omega_6$
Tm³⁺							
³ F ₂ → ³ H ₆	H	670	0	0	0.2550	0	$\eta \cdot 0.2550\Omega_6$
³ F ₃ → ³ H ₆	H	695	0	0.3164	0.8413	0	$\eta(0.3164\Omega_4 + 0.8413\Omega_6)$
³ H ₄ → ³ H ₆	L	800	0.2357	0.1081	0.5916	0	$\eta(0.2357\Omega_2 + 0.1081\Omega_4 + 0.5916\Omega_6)$

JOLIR applet

<https://omasgroup.org/jolir-interactive-software/>

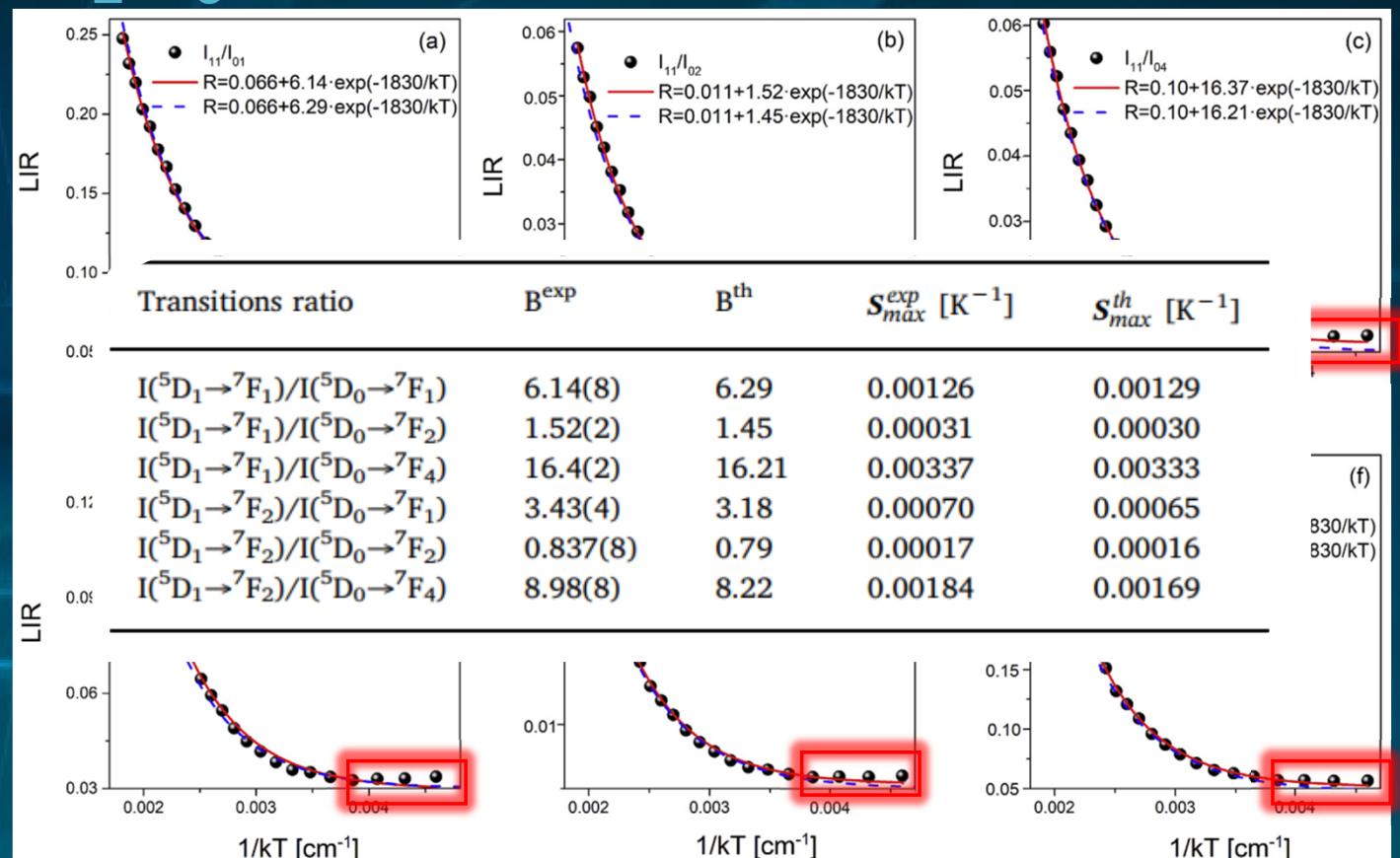
Magnetic dipole
 and electric
 quadrupole
 transitions in the
 trivalent lanthanide
 series: Calculated
 emission rates and
 oscillator strengths,
 doi:
 10.1103/PhysRevB.8
 6.125102



58 Ce Cerium 140.116	59 Pr Praseodymium 140.908	60 Nd Neodymium 144.243	61 Pm Promethium 144.913	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.925	66 Dy Dysprosium 162.500	67 Ho Holmium 164.930	68 Er Erbium 167.259	69 Tm Thulium 168.934	70 Yb Ytterbium 173.055
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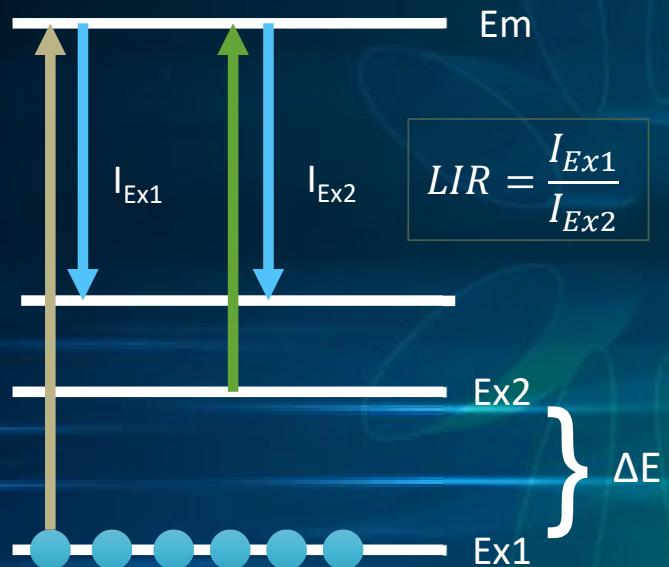
Testing on $\text{Y}_2\text{O}_3:\text{Eu}^{3+}$

- LIR of ${}^5\text{D}_1 \rightarrow {}^7\text{F}_{1,2}$ and ${}^5\text{D}_0 \rightarrow {}^7\text{F}_{1,2,4}$
- $$LIR = C \frac{\alpha A_R + M \rho g_2 n^p}{\beta A_R + M \rho g_1 (1+n)^p}$$
- R. Geitenbeek, H.W. de Wijn, A. Meijerink, doi: 10.1103/PhysRevApplie d.10.064006



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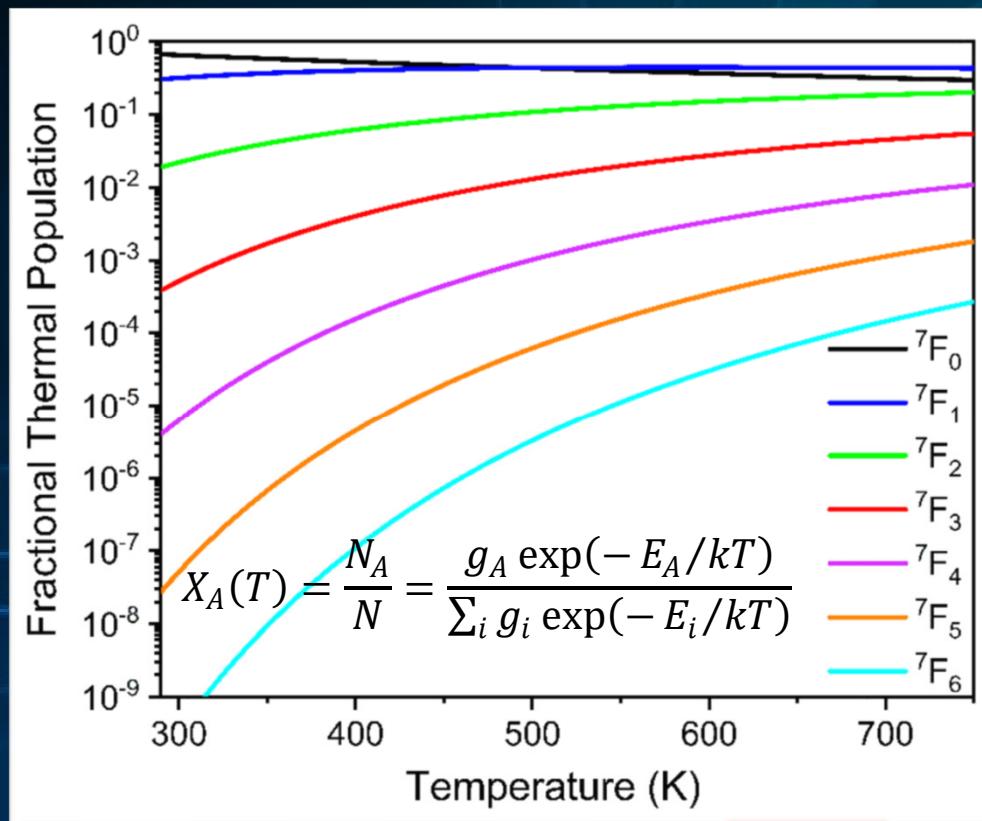
Dual-excited single band LIR



- A.Souza,..., R. Ferreira, L.D. Carlos, O.L. Malta, High-sensitive Eu³⁺ ratiometric thermometers based on excited state absorption with predictable calibration, doi: 10.1039/C6NR00158K
- At 0 K all optical centers are at ground.
- T > 0K : thermal population.
- Excitation from Ex1 and Ex2.
- Single emission is monitored.
- LIR of two emissions by excitations from Ex1 and Ex2.
- Dual-excited – much larger ΔE → larger S_r

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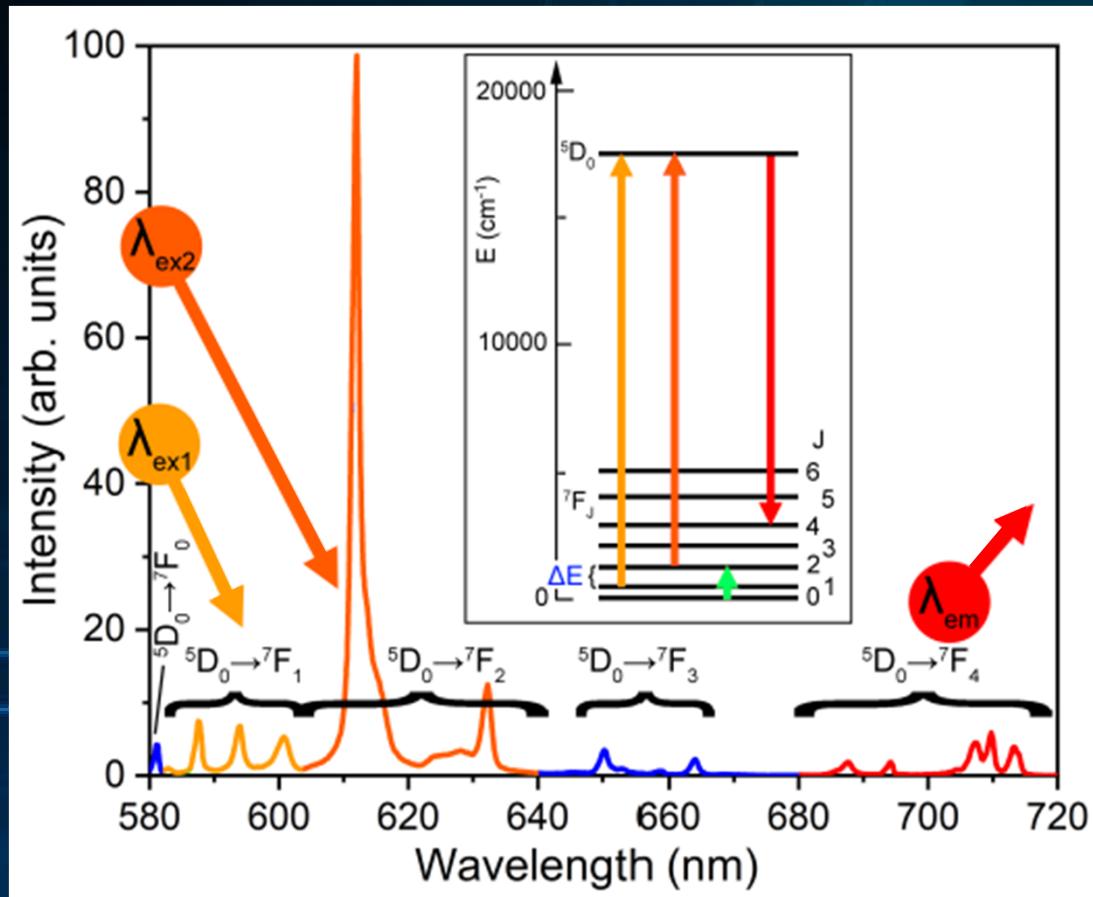
How? Optical centers redistribution



- Eu^{3+} ion example.
- 7F_J are thermally excited.
- Number of optical centers follows Boltzmann distribution.
- Excitation can be executed on higher levels of the ground multiplet.

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How? Excitations and emission



- Excitations from 7F_1 and 7F_2
- Monitor emission to 7F_4

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Judd-Ofelt model

$$A_\lambda = \frac{64\pi^4 \tilde{\nu}_\lambda^3}{3h} \chi_{ED} D_{ED}^\lambda \quad A_{MD} = \frac{64\pi^4 \tilde{\nu}_{MD}^3}{3h} \chi_{MD} D_{MD}$$



$$I_{SLJ \rightarrow S'L'J'} = h\tilde{\nu}_{SLJ \rightarrow S'L'J'} N_{SLJ} A_{SLJ \rightarrow S'L'J'}$$

$$LIR = \frac{I_1}{I_2} = B \exp\left(\frac{\Delta E}{kT}\right)$$

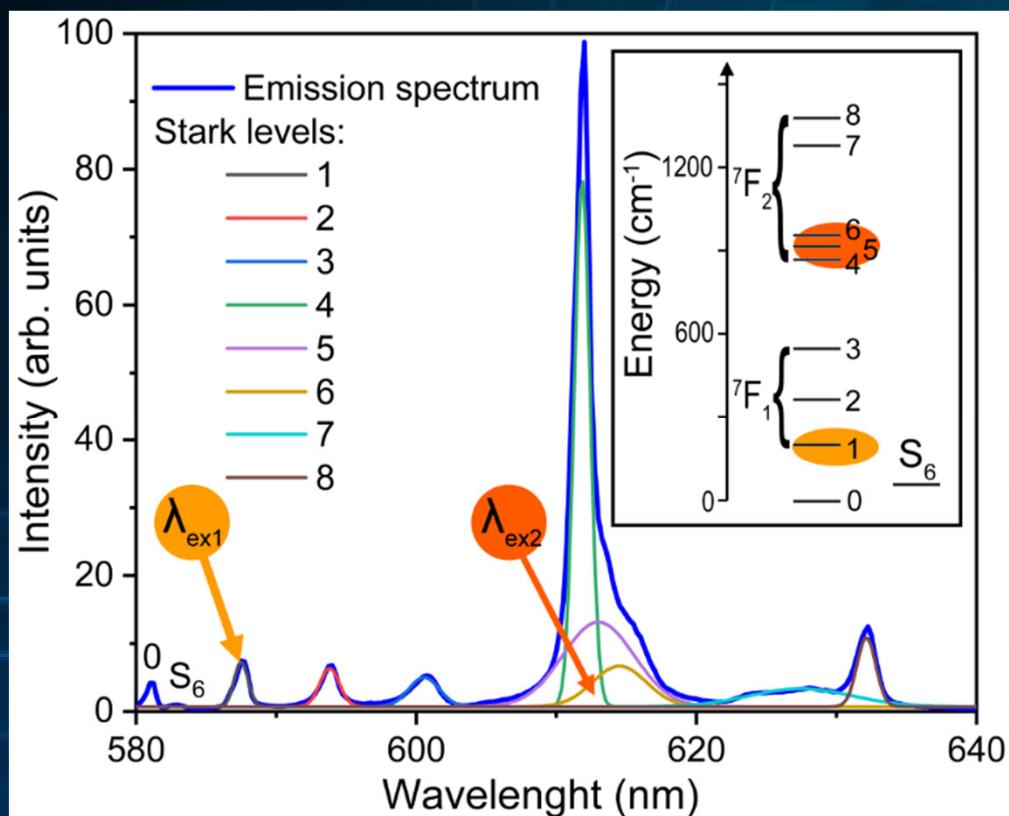


$$B_{JO} = \left(\frac{\nu_1}{\nu_2}\right)^4 \frac{n_1^3 \cdot 9.6 \cdot 10^{-42} \text{ esu}^2 \text{ cm}^2}{e^2 \Omega_2 U^2 \cdot n_2 (n_2^2 + 2)^2 / 9}$$

- Prediction of the B parameter.
- $D_{ED}^\lambda = e^2 \Omega_\lambda U^\lambda$
- $D_{MD} = 9.6 \cdot 10^{-42} \text{ esu}^2 \text{ cm}^2$
- ΔE can be obtained from spectrum.

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Corrections



- Excitations are performed in some Stark sublevels.
 - Correction factors are needed:
- $$\varphi_1 = \frac{I_{1,1}}{\sum_{j=1}^3 I_{1,j}}, \varphi_2 = \frac{\sum_{j=4}^6 I_{2,j}}{\sum_{j=4}^8 I_{2,j}}$$
- $LIR_{JO} = \frac{\varphi_1}{\varphi_2} B_{JO} \exp\left(\frac{\Delta E_{sp}}{kT}\right)$

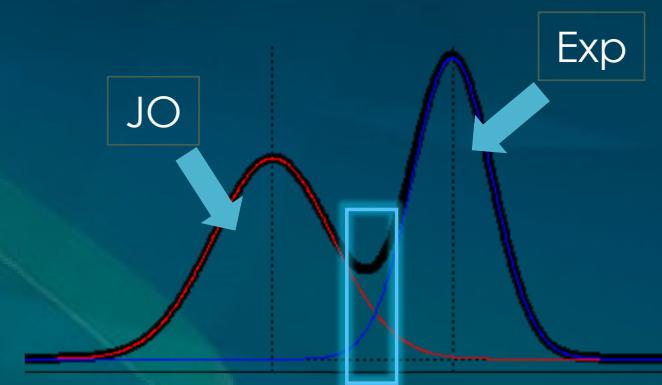
Judd-Ofelt modelling of the dual-excited single band ratiometric luminescence thermometry, A. Ćirić, I. Zeković, M. Medić, Ž. Antić, M.D. Dramićanin, doi: [10.1016/j.jlumin.2020.117369](https://doi.org/10.1016/j.jlumin.2020.117369)

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TEST ON $\text{Lu}_2\text{O}_3:\text{Eu}^{3+}$

$$\bullet B = 0.04773$$

- $\varphi_1 = 0.304, \varphi_2 = 0.873$
- **JOES:** $\Omega_2 = 9.605 \cdot 10^{-20} \text{ cm}^2, \Omega_4 = 2.928 \cdot 10^{-20} \text{ cm}^2$
[https://omasgroup.org/joes – software/](https://omasgroup.org/joes-software/)
- $B_{JO} = 0.137$
- $B_{JO} \frac{\varphi_1}{\varphi_2} = 0.04770$
- **99.9%** match between B and $B_{JO} \frac{\varphi_1}{\varphi_2}$



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CONCLUSIONS

- Temperature invariant B parameter for LIR can be predicted
 - Prediction of Sensitivities!
- Needed: 1 RT spectrum or Ω from literature!
- Test showed high matching between experimental and theoretical B parameters.
- Applicability: tool for initial selection of phosphors!
- Applies to other Lanthanides.

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Thank You!

Software:

<https://omasgroup.org/jolr-interactive-software/>

<https://omasgroup.org/joes-software/>

University of Belgrade
OMAS group
omasgroup.org